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INTEGRATED 6-DOF SPACECRAFT ORBIT-ATTITUDE DYNAMICS MODELING AND ITS
APPLICATION IN HOVERING CONTROL OVER AN ASTEROID**Abstract**

Recent studies have shown that orbital and attitude motions of spacecraft are dynamically coupled in close proximity of small asteroids through the gravity. Generally, the gravitational orbit-attitude coupling is more significant with a larger ratio of the spacecraft's size to the orbital radius. More importantly, the close-proximity operations about asteroids usually require that the relative position and attitude of the spacecraft follow the reference trajectory simultaneously. Therefore, integrated 6-DOF orbit-attitude control yields better performance than the classical separate control scheme in terms of both accuracy and agility.

One challenge in the design of integrated 6-DOF orbit-attitude motion control is to find an adequate unified mathematical representation for the 6-DOF motion, which must be amenable for the application of nonlinear control theories, and is also required to be free of singularities and be applicable to a wide range of close-proximity operations. As for the representation of the 6-DOF orbit-attitude motion, the spacecraft can be considered as a rigid body, and the configuration space is the Lie Group $SE(3)$, which is the set of position and attitude of the spacecraft. Recently, exponential coordinates of the Lie Group $SE(3)$ have been used in the representation of the 6-DOF rigid body motion and the controller design. Exponential coordinates have several advantages: Free of singularity, has a vector form, convenient for the controller design, and can achieve almost global convergence in the controller. However, exponential coordinates of $SE(3)$ have been used only in the spacecraft's kinematics, that is, only the relation between the first-order time derivative of exponential coordinates and the spacecraft's (angular) velocity has been given.

In this paper, we will improve current modeling method by using exponential coordinates of $SE(3)$ on the dynamical level further, that is, by giving the relation between the second-order time derivative of exponential coordinates and the spacecraft's (angular) acceleration. By using this relation on the dynamical level, the system can be written as a second-order system with a compact form. Then, it becomes more convenient for controller design, and many control theories can be easily applied to this second-order system. Finally, based on the second-order system, a controller for hovering over an asteroid with almost global convergence and robustness is designed by using sliding mode control, and is verified by using numerical simulations.